

DETAILS EXPLANATIONS**[PART : A]****1. Base load plants :**

- Hydro electric plant
- Nuclear power plant
- Coal based thermal power plant

Peak Load Plants :

- Diesel power plant
- Pumped storage plant
- Gas power plant

2. Hydro turbines are classified as :

- Kaplan — High specific speed
- Francis — Medium specific speed
- Pelton — Low specific speed

3. In pumped storage plant reversible turbine are used which operate as turbine for power generation during peak load and operate as a pump for pumping the water during peak off load.**4. Nuclear fuels are classified as :**

- **Fertile** : It is not self fissionable.
Example : Uranium 238, Thorium 232.
- **Fissile** : By thermal neutrons fertile can be converted into fissile material.

Example : Uranium 235, Plutonium 239**5. Feeders are designed according to current carrying capacity and distributors are designed according to voltage drop.****6. Due to Skin effect on solid conductor :**

- Conductor resistance increase.
- Effective cross sectional area reduces.

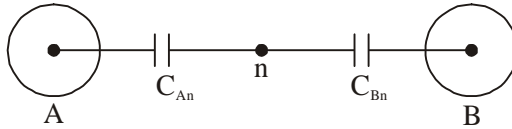
7. Internal flux linkage

$$\lambda_{in} = \frac{\mu I}{8\pi} \text{ Wb-T/m}$$

External flux linkage

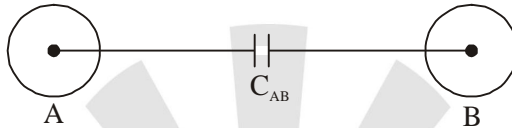
$$\lambda_{ext} = \frac{\mu I}{2\pi} \ln \frac{d}{r} \text{ Wb-T/m}$$

8. For single phase two wire line.



Line to neutral capacitance

$$C_{An} = C_{Bn} = \frac{2\pi\epsilon}{\ln\left(\frac{d}{r}\right)}$$



Line to line capacitance

$$C_{AB} = C_{An}/2 = \frac{\pi\epsilon}{\ln\left(\frac{d}{r}\right)}$$

- 9.
- A → unitless
 - B → ohm
 - C → mho or Siemens
 - D → unitless

10. $P_c = \frac{240}{\delta} (f + 25) \sqrt{\frac{r}{d}} (V - V_D)^2 \times 10^{-5}$ kW/km/phase
 where, V = Operating voltage

V_D = Disruptive critical voltage

r = Radius of conductor

d = Distance between conductor

f = Operating frequency

δ = Air density factor

11. To improve string efficiency following methods are used :

- Using longer cross-arm
- Using insulation grading.
- Using guard ring.

12. For solid double line to ground fault, fault impedance $z_f = 0$.

$V_{a1} = V_{a2} = V_{a0}$ i.e., all sequential network are connected in parallel.

13. In percentage differential relay the ratio of number of turns of restraining coil and operating coil i.e. $\frac{N_r}{N_o}$ decide a particular percentage of average current to operate the relay.
14. To prevent arc restriking due to transient recovery voltage (TRV) Cassie theory is given, according to which "If rate of heat dissipation between circuit breaker contacts is greater than rate of heat developed by arc then arc will not restrike."
15. Bundled conductor increase the effective radius i.e., geometrical mean radius which increase the corona starting voltage i.e., disruptive critical voltage so less corona formation and less power loss.
16. $r = \frac{1}{2} \sqrt{\frac{L}{C}} = \frac{1}{2} \sqrt{\frac{20 \times 10^{-3}}{0.02 \times 10^{-6}}} = 500 \Omega$
17. To prevent false tripping due to inrush current in transformer :
- Some intentional time delay provide to relay.
 - Harmonic restraint relay used for second harmonic in inrush current.
18. For open ended line $Z_L = \infty$
Current reflection coefficient

$$\tau_1 = \frac{Z_0 - Z_L}{Z_0 + Z_L} = \frac{Z_L \left(\frac{Z_0}{Z_L} - 1 \right)}{Z_L \left(\frac{Z_0}{Z_L} + 1 \right)} = \frac{0 - 1}{0 + 1} = -1$$

19. With increase in temperature increase in length of conductor so sag will also increase.
20. For resonance

$$X_L = \frac{X_C}{3}$$

$$\omega L = \frac{1}{3\omega C}$$

$$L = \frac{1}{3\omega^2 C}$$

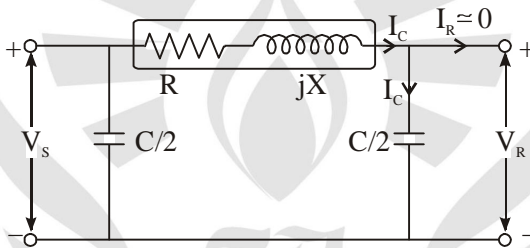
$$L = \frac{1}{12\pi^2 f^2 C}$$

[PART : B]

21. • Superheater dry the steam coming out from boiler and also increase the temperature using heat from flue gases.
 • Economiser heat the feed water with the heat from flue gases and its way to boiler.
 • Airpreheater extract the remaining heat from flue gases and give it to the air having supplied to furnace for cooling and combustion.

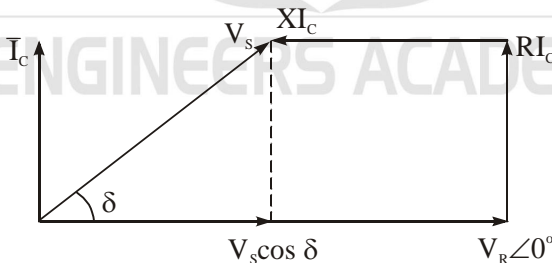
22. Ferranti effect occurs

- At no load or light load condition.
- Due to shunt capacitance.
- In medium and long transmission line.
- $|V_{R_{no\ load}}| > |V_S|$
- Insulation may damage so shunt reactor used to prevent ferranti effect.



$$\therefore \bar{I}_C = j\omega \frac{C}{2} \bar{V}_R$$

\bar{I}_C leads \bar{V}_R by angle 90° .



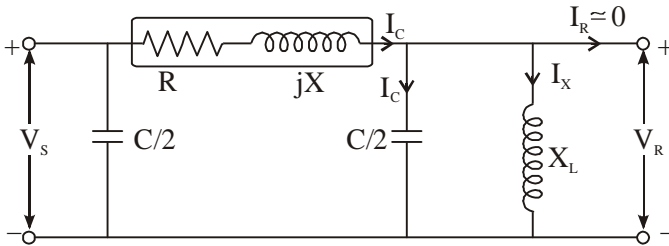
Apply KVL in loop

$$\bar{V}_S = \bar{V}_R + R\bar{I}_C + jX\bar{I}_C$$

From phasor diagram

$$|V_{R_{no\ load}}| > |V_S|$$

i.e., ferranti effect



$$\therefore \bar{I}_X = \frac{\bar{V}_R}{jX_L}$$

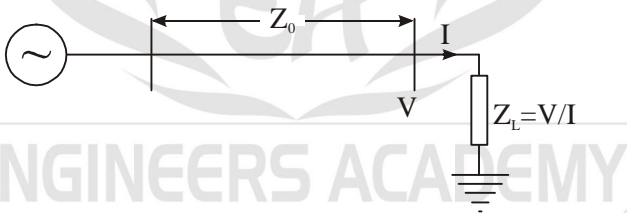
\bar{I}_X lags \bar{V}_R by angle 90°



$$\therefore \bar{I} = \bar{I}_C + \bar{I}_X = 0$$

So, $|V_{R|_{no\ load}}| = |V_S|$

23. Surge impedance loading provides ideal power transfer capability using flat voltage profile.



Case-I : If $Z_L = Z_0$

$$\Rightarrow \frac{V}{I} = \sqrt{\frac{L}{C}}$$

$$\Rightarrow \omega C V^2 = \omega L I^2$$

$$\Rightarrow Q_C = Q_L$$

Net $VAr = Q_L - Q_C$

$$\Rightarrow Q = 0$$

$$\Rightarrow \Delta V = 0$$

$$\Rightarrow V_S - V_R = 0$$

$$\Rightarrow V_S = V_R$$

i.e., flat voltage profile.

Case-II : If $Z_L < Z_0$

$$\Rightarrow \frac{V}{I} < \sqrt{\frac{L}{C}}$$

$$\Rightarrow Q_C < Q_L$$

$$\text{Net VAR} = Q_L - Q_C$$

$$\Rightarrow Q > 0$$

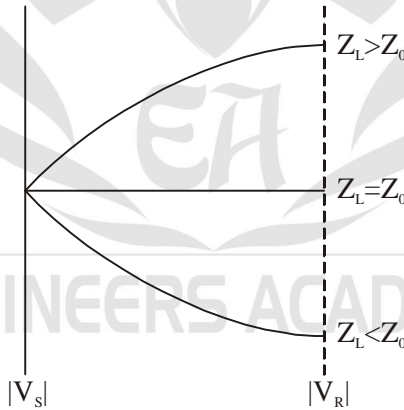
$$\Rightarrow \Delta V > 0$$

$$\Rightarrow V_S > V_R$$

i.e., voltage drop along the line.

Case-III : If $Z_L > Z_0$

$$\Rightarrow \frac{V}{I} > \sqrt{\frac{L}{C}}$$



$$\Rightarrow Q_C > Q_L$$

$$\text{Net VAR} = Q_L - Q_C$$

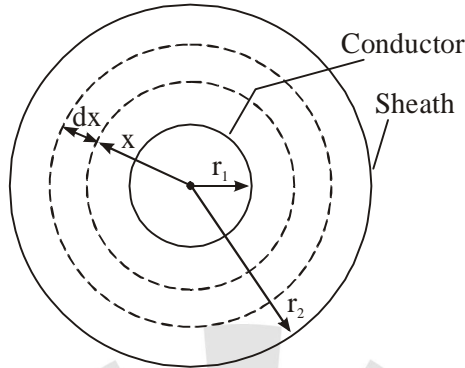
$$\Rightarrow Q < 0$$

$$\Rightarrow \Delta V < 0$$

$$\Rightarrow V_S < V_R$$

i.e., voltage rise along the line.

24. Insulation resistance of cable :



r_1 = Radius of conductor.

r_2 = Radius of sheath with conductor.

Insulation between conductor and outer metallic sheath at distance x from centre.

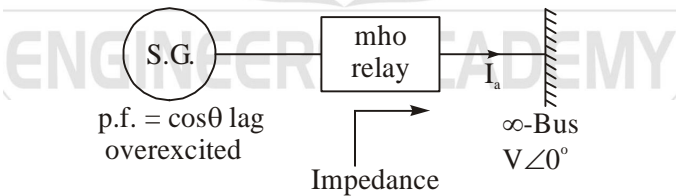
$$\therefore R = \frac{\rho l}{A}$$

So,
$$dR = \rho \frac{dx}{2\pi x l}$$

$$\Rightarrow R = \frac{\rho}{2\pi l} \int_{r_1}^{r_2} \frac{1}{x} dx$$

$$\Rightarrow R = \frac{\rho}{2\pi l} \ln\left(\frac{r_2}{r_1}\right)$$

25.

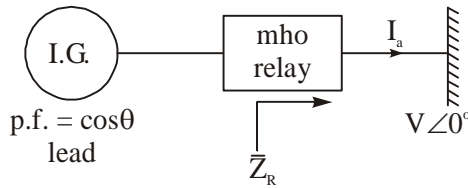


Impedance seen by mho relay

$$\begin{aligned} \bar{Z}_R &= \frac{\bar{V}}{\bar{I}_a} = \frac{V\angle 0^\circ}{I_a\angle -\theta} \\ &= Z_1\angle\theta \text{ i.e., Inductive} \\ &= R_1 + jX_1 \text{ so no tripping.} \end{aligned}$$

If excitation fails $E \propto I_f = 0$

On the failure of excitation synchronous generator behaves as induction generator due to presence of damper bar, so it starts taking magnetising current from supply. And hence it starts operating at leading p.f.



$$\bar{Z}_R = \frac{V \angle 0^\circ}{I_a \angle +\theta}$$

= $Z_2 \angle -\theta$ i.e., capacitive so tripping

$$= R_2 - jX_2$$

26. $\therefore P = V I \cos \theta$

If a particular power is transmitted at a particular voltage.

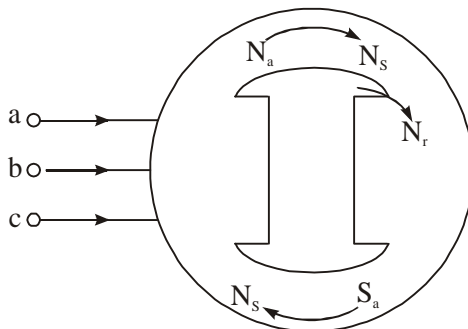
$$\downarrow I \propto \frac{1}{\cos \theta \uparrow}$$

Following are advantages of power factor improvement :

- $\downarrow S = VI \downarrow$ for same output power less KVA required so size of machines and cost reduces.
- To carry less current the cross-sectional area of conductor requirement reduces and hence transmission cost reduces.
- Transmission line loss I^2R reduces so efficiency increase.
- Voltage drop $\Delta V = IZ$ reduces along the line so voltage regulation reduces.

27. Symmetrical component are used for unsymmetrical fault analysis.

- **Positive Sequence Current :**

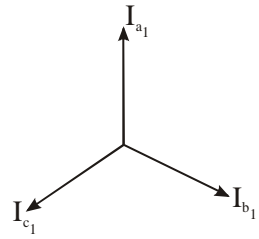


The sequence of current corresponding to which armature flux ϕ_a or mmf F_a rotates in the same direction of rotor, is called positive sequence current.

$$I_{a_1} = I \angle 0^\circ$$

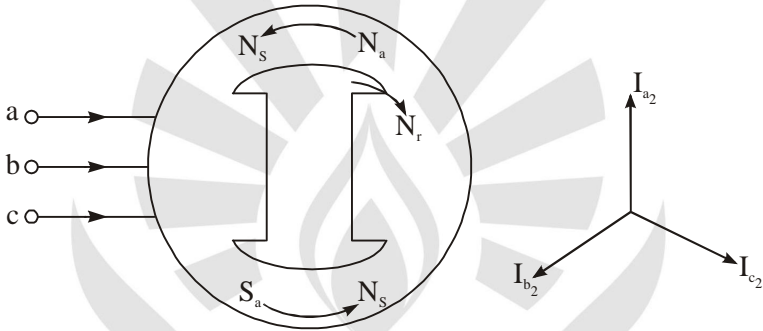
$$I_{b_1} = I \angle -120^\circ = \alpha^2 I_{a_1}$$

$$I_{c_1} = I \angle +120^\circ = \alpha I_{a_1}$$



- Negative Sequence Current**

The sequence of current corresponding to which armature flux ϕ_a or mmf F_a rotates in the opposite direction of rotor, is called negative sequence current.



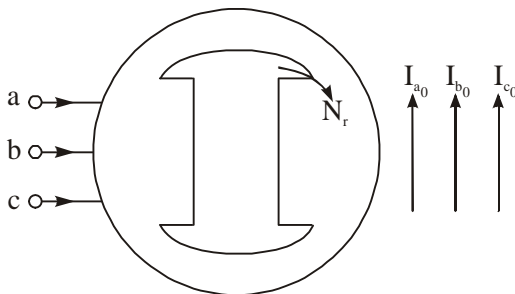
$$I_{a_2} = I \angle 0^\circ$$

$$I_{b_2} = I \angle +120^\circ = \alpha I_{a_2}$$

$$I_{c_2} = I \angle -120^\circ = \alpha^2 I_{a_2}$$

- Zero Sequence Current :**

The sequence of current corresponding to which no rotating field develop only armature leakage flux is there, called zero sequence current.

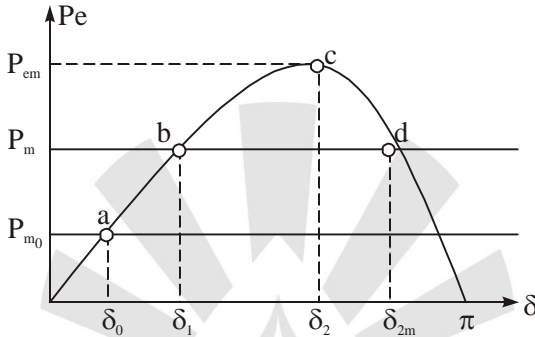


$$I_{a_0} = I|_{0^\circ}$$

$$I_{b_0} = I|_{0^\circ} = I_{a_0}$$

$$I_{c_0} = I|_{0^\circ} = I_{a_0}$$

28. For sudden change in shaft input or mechanical input from P_{m_0} to P_m .



From δ_0 to δ_1 due to increase in input there is acceleration in rotor of alternator and from δ_1 to δ_2 deceleration in rotor speed and finally this swinging of rotor from δ_0 to δ_2 will settle down to δ_1 due to damper bar presence.

From swing equation

$$P_a = M \frac{d^2\delta}{dt^2}$$

$$\Rightarrow \frac{d^2\delta}{dt^2} = \frac{P_a}{M}$$

$$\int 2 \frac{d\delta}{dt} \frac{d^2\delta}{dt^2} dt = \int \frac{P_a}{M} 2 \frac{d\delta}{dt} dt$$

$$\int \frac{d}{dt} \left(\frac{d\delta}{dt} \right)^2 dt = \frac{2}{M} \int P_a d\delta$$

$$\left(\frac{d\delta}{dt} \right)^2 \Big|_{\delta_0}^{\delta_2} = \frac{2}{M} \int_{\delta_0}^{\delta_2} P_a d\delta$$

$$\left(\frac{d\delta}{dt} \right)^2 \Big|_{\delta_2} - \left(\frac{d\delta}{dt} \right)^2 \Big|_{\delta_0} = \frac{2}{M} \int_{\delta_0}^{\delta_2} P_a d\delta$$

$$\text{At } \delta_2 \text{ maximum swing angle } \frac{d\delta}{dt} = 0$$

At δ_0 minimum swing angle $\frac{d\delta}{dt} = 0$

$$0 - 0 = \frac{2}{M} \int_{\delta_0}^{\delta_2} p_a d\delta$$

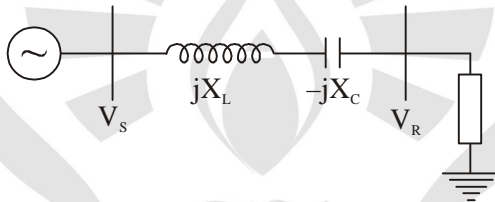
$$\int_{\delta_0}^{\delta_2} p_a d\delta = 0$$

$$\int_{\delta_0}^{\delta_1} p_a d\delta + \int_{\delta_1}^{\delta_2} p_a d\delta = 0$$

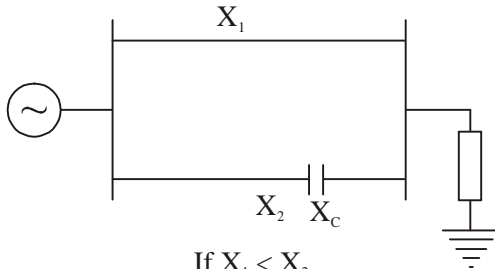
$$\int_{\delta_0}^{\delta_1} (p_m - p_e) d\delta = \int_{\delta_1}^{\delta_2} (p_e - p_m) d\delta$$

Accelerating area = Deaccelerating Area
i.e., Equal area criterion.

29. With series capacitive compensation Following advantage occur:



- Steady state stability limit $P_{\max} = \frac{V_S V_R}{(X_L - X_C)}$ increases due to decrease in series reactance.
- With increase in P_{\max} the operating power angle δ also reduces so transient stability limit also increases.
- In double circuit transmission line by using series capacitor equal load division can be supplied.



If $X_1 < X_2$
then $X_1 = (X_2 - X_C)$

- Surge impedance loading i.e., ideal power transfer capability of line increases.

30. $\therefore fl = 50 \times 200 = 10,000 \text{ Hz-km}$

As $4000 < fl < 12000$ so it is a medium transmission line.

$$\begin{aligned} \therefore A &= 1 + \frac{YZ}{2} = 1 + \frac{(j\omega cl)(j\omega Ll)}{2} \\ &\left(\because \text{For lossless line } \begin{array}{l} r \approx 0 \\ g = 0 \end{array} \right) \\ &= 1 - \frac{\omega^2 l^2 LC}{2} = 1 - \frac{\omega^2 l^2}{2V_C^2} \quad \left(\because V_C = \frac{1}{\sqrt{LC}} \right) \\ &= 1 - \frac{1}{2} \left[\frac{2\pi(50) \times 200}{3 \times 10^5} \right]^2 \\ &\quad (\because V_C = 3 \times 10^5 \text{ km/sec}) \\ &= 0.978 \end{aligned}$$

$$\therefore |V_R|_{\text{no load}} = \left| \frac{V_S}{A} \right| = \frac{220}{0.978} = 224.95 \text{ kV}$$

31. For the safety of the person working in neighbourhood of machine the body of machine is earthed through earth electrode and the value of resistance of earth electrode should be minimum for safety purpose.

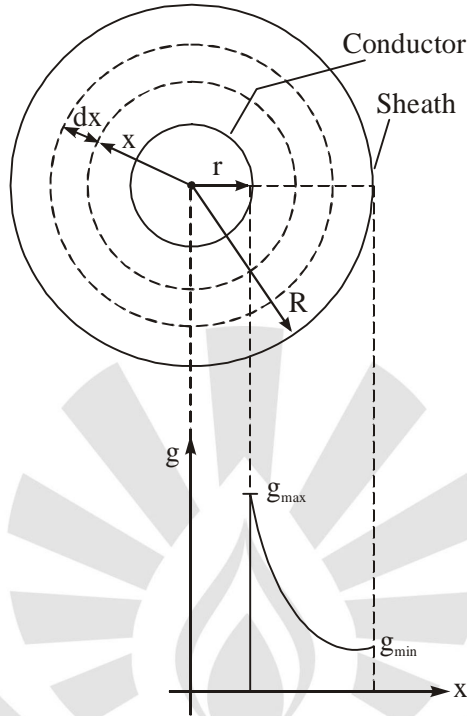
The value of resistance of earth electrode depends upon :

- Shape and size of earth electrode.
- Depth in the soil of earth electrode.
- Material of earth electrode.
- Soil condition i.e., ph value.

32. **Following are advantage of SF₆ circuit breaker:**

- SF₆ gas provides higher dielectric strength (up to three times of air) at normal pressure, so less electrical clearance is required for arc extinction.
- Its heat transfer ability is higher. (Upto 2.5 times that of air)
- It is highly inert gas so does not form explosive mixture with air.
- It is chemically stable so does not get decomposed into gases.
- Its dielectric strength builds up at very fast rate So auxillary braking not required to reduce RRRV.

33. Electrostatic stress in single core cable :-



r = Radius of conductor

R = Radius of sheath with conductor.

At a distance x from centre of conductor of cable electric field intensity.

$$E_x = \frac{Q}{2\pi \epsilon_0 \epsilon_r x} \text{ V/m}$$

Potential gradient or Dielectric strength

$$g = E_x = \frac{Q}{2\pi \epsilon_0 \epsilon_r x} \text{ V/m} \dots(1)$$

Potential of conductor with respect to sheath

$$V = \int g dx = - \int_R^r E_x dx$$

$$\Rightarrow V = \frac{Q}{2\pi \epsilon_0 \epsilon_r} \ln\left(\frac{R}{r}\right)$$

$$\Rightarrow Q = \frac{2\pi \epsilon_0 \epsilon_r V}{\ln(R/r)}$$

equation (1)

$$g = \frac{2\pi \epsilon_0 \epsilon_r V}{\ln(R/r)} \cdot \frac{1}{2\pi \epsilon_0 \epsilon_r x}$$

$$\Rightarrow g = \frac{V}{x \ln(R/r)}$$

$$\Rightarrow g_{\max} = \frac{V}{x_{\min} \ln(R/r)} = \frac{V}{r \ln(R/r)}$$

$$\Rightarrow g_{\min} = \frac{V}{x_{\max} \ln(R/r)} = \frac{V}{R \ln(R/r)}$$

In order to keep a fixed overall size of conductor (R) for a particular voltage V, radius of conductor for minimum value of g_{\max} .

$$\frac{d}{dr} \{r \ln R/r\} = 0$$

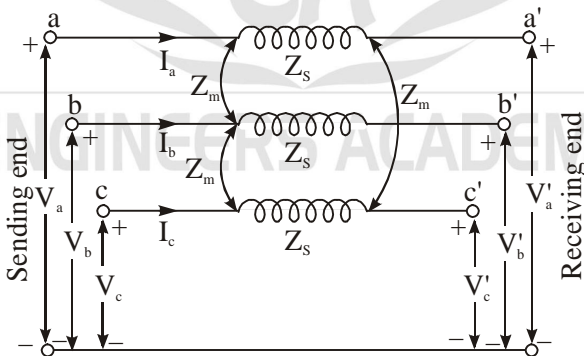
$$\Rightarrow r \cdot \frac{r}{R} \cdot \left(-\frac{R}{r^2}\right) + \ln\left(\frac{R}{r}\right) \cdot 1 = 0$$

$$\Rightarrow \ln\left(\frac{R}{r}\right) = 0$$

$$\Rightarrow \frac{R}{r} = e$$

i.e., condition for economic size of conductor.

34. Sequential network of transmission line :



Voltage drop along the line

$$\Rightarrow V_a - V_a' = Z_s I_a + Z_m I_b + Z_m I_c$$

$$\Rightarrow V_b - V_b' = Z_m I_a + Z_s I_b + Z_m I_c$$

$$\Rightarrow V_c - V_c^1 = Z_m I_a + Z_m I_b + Z_s I_c$$

$$\Rightarrow \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} - \begin{bmatrix} V_a^1 \\ V_b^1 \\ V_c^1 \end{bmatrix} = \begin{bmatrix} Z_s & Z_m & Z_m \\ Z_m & Z_s & Z_m \\ Z_m & Z_m & Z_s \end{bmatrix} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix}$$

$$\Rightarrow V_p - V_p^1 = Z I_p$$

$$\Rightarrow AV_s - AV_s^1 = Z(AI_s)$$

$$\Rightarrow V_s - V_s^1 = (A^{-1}ZA)I_s$$

$$\Rightarrow \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} - \begin{bmatrix} V_{a1}^1 \\ V_{a2}^1 \\ V_{a0}^1 \end{bmatrix} = \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$\therefore Z_{seq} = A^{-1}ZA$$

$$= \frac{1}{3} \begin{bmatrix} 1 & \alpha & \alpha^2 \\ 1 & \alpha^2 & \alpha \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} Z_s & Z_m & Z_m \\ Z_m & Z_s & Z_m \\ Z_m & Z_m & Z_s \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} Z_s - Z_m & 0 & 0 \\ 0 & Z_s - Z_m & 0 \\ 0 & 0 & Z_s + 2Z_m \end{bmatrix} \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix}$$

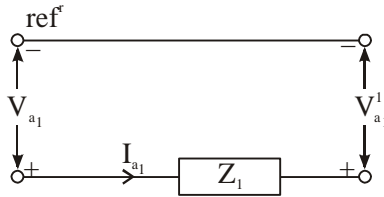
$$\Rightarrow \begin{bmatrix} V_{a1} \\ V_{a2} \\ V_{a0} \end{bmatrix} - \begin{bmatrix} V_{a1}^1 \\ V_{a2}^1 \\ V_{a0}^1 \end{bmatrix} = \begin{bmatrix} Z_1 & 0 & 0 \\ 0 & Z_2 & 0 \\ 0 & 0 & Z_0 \end{bmatrix} \begin{bmatrix} I_{a1} \\ I_{a2} \\ I_{a0} \end{bmatrix}$$

$$V_{a1} - V_{a1}^1 = Z_1 I_{a1} \quad \dots(1)$$

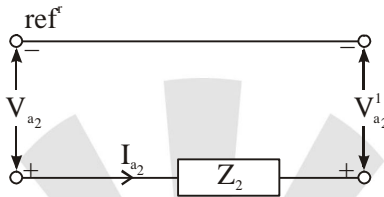
$$V_{a2} - V_{a2}^1 = Z_2 I_{a2} \quad \dots(2)$$

$$V_{a0} - V_{a0}^1 = Z_0 I_{a0} \quad \dots(3)$$

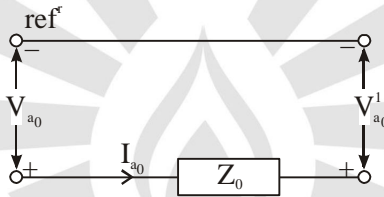
From equation (1) : Positive sequence network



From equation (2) : Negative sequence network



From equation (3) : Zero sequence network



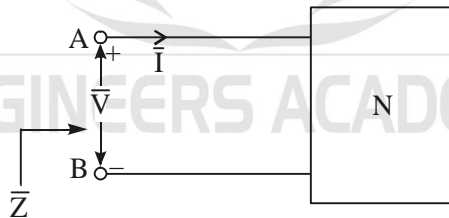
Here, $Z_1 = Z_2 = Z_s - Z_m$

$Z_0 = Z_s + 2Z_m$

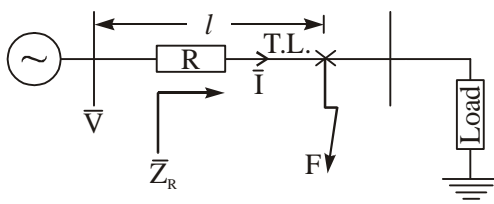
Where, Z_s = Self impedance of line.

Z_m = Mutual impedance between line.

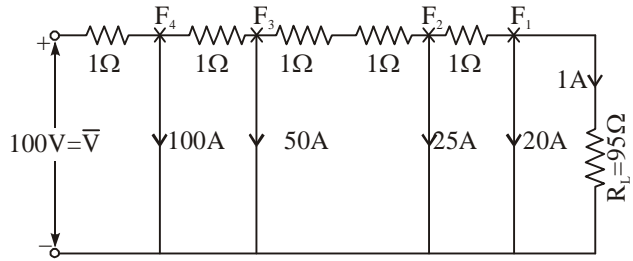
35. Distance relay is used for protection of transmission line.



$\bar{Z} = \frac{\bar{V}}{\bar{I}}$ i.e., impedance seen from AB



$$\text{Impedance seen by relay } \bar{Z}_R = \frac{\bar{V}}{\bar{I}}$$



- In the normal condition impedance seen by relay is higher i.e. load impedance as well as transmission line impedance.
- In the fault condition impedance seen by relay reduces and it depends upon distance of fault.
- **Impedance Relay** : (Voltage restraint overcurrent relay)

$$T = k_1 |I|^2 - k_2 |V|^2$$

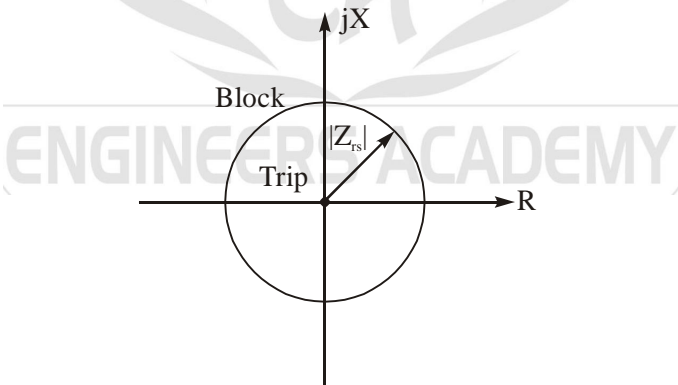
$$\Rightarrow \frac{|V|}{|I|} < \frac{k_1}{k_2}$$

$$|Z| < |Z_{rs}|$$

$$|R + jX| < |Z_{rs}|$$

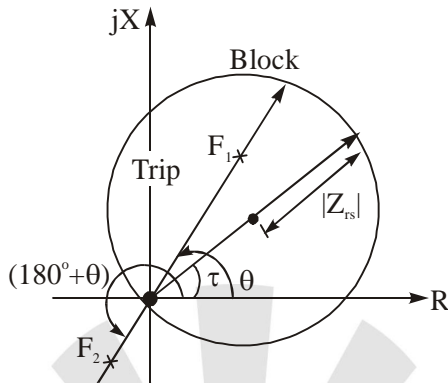
$$R^2 + X^2 < |Z_{rs}|^2$$

i.e. equation of circle.



- The relay operates if fault on either side within a particular distance ' l_R ' (reach of relay) i.e., distance relay. So it is non-directional relay.

- **Mho Relay or Modified Impedance Relay** : (Voltage restraint directional relay)



$$T = K_3|V||I|\cos(\theta - \tau) - K_2|V|^2$$

Relay operates if

$$K_3|V||I|\cos(\theta - \tau) > K_2|V|^2$$

$$\Rightarrow \frac{|V|}{|I|} < 2\left(\frac{K_3}{2K_2}\right)\cos(\theta - \tau)$$

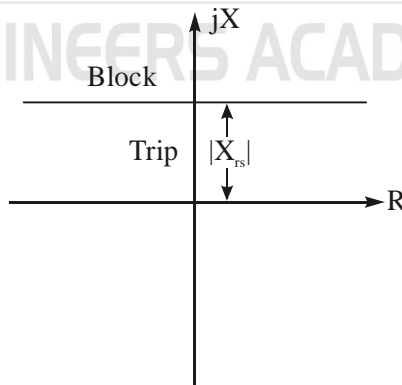
$$\Rightarrow |Z| < 2|Z_{rs}|\cos(\theta - \tau)$$

F_1 at a particular distance detect and F_2 does not detect. So it detects fault within a particular distance in a particular direction.

- **Reactance Relay** : (Directional restraint overcurrent relay)

$$T = K_1|I|^2 - K_3|V||I|\cos(\theta - \tau)$$

Relay operates if



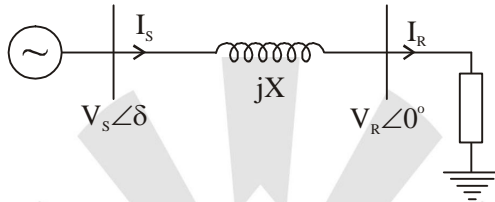
$$K_1|I|^2 > K_3|V||I|\cos(\theta - 90^\circ) \quad [\because \tau = 90^\circ]$$

$$\Rightarrow \frac{|V|}{|I|} \sin \theta < \frac{K_1}{K_3}$$

$$\Rightarrow |Z| \sin \theta < \frac{K_1}{K_3}$$

$$\Rightarrow |X| < |X_{rs}|$$

36. For loss less short transmission line



$$\bar{Z} = jX = X|90^\circ$$

$$A = D = 1$$

$$B = Z = X|90^\circ$$

$$C = 0$$

$$\therefore \bar{V}_S = \bar{V}_R + jX\bar{I}_R$$

$$\Rightarrow \bar{I}_R = \frac{V_S}{X} \angle \delta - 90^\circ - \frac{V_R}{X} \angle -90^\circ$$

$$\Rightarrow \bar{I}_R^* = \frac{V_S}{X} \angle 90^\circ - \delta - \frac{V_R}{X} \angle 90^\circ$$

$$\therefore \bar{S}_R = \bar{V}_R \bar{I}_R^*$$

$$\Rightarrow P_R + jQ_R = \frac{V_S V_R}{X} \angle 90^\circ - \delta - \frac{V_R^2}{X} \angle 90^\circ$$

$$\therefore P_R = \frac{V_S V_R}{X} \cos(90^\circ - \delta) - \frac{V_R^2}{X} \cos 90^\circ$$

$$\Rightarrow P_R = \frac{V^2}{X} \sin \delta \quad \dots(1)$$

$$[\because |V_S| = |V_R| = V]$$

$$\therefore Q_R = \frac{V_S V_R}{X} \sin(90^\circ - \delta) - \frac{V_R^2}{X} \sin 90^\circ$$

$$\Rightarrow Q_R = \frac{V^2}{X} \cos \delta - \frac{V^2}{X} \quad \dots(2)$$

$$\therefore \bar{I}_S = C\bar{V}_R + D\bar{I}_R$$

$$\Rightarrow \bar{I}_S = \bar{I}_R$$

$$\Rightarrow \bar{I}_S^* = \bar{I}_R^* = \frac{V_S}{X} |90^\circ - \delta - \frac{V_R}{X} |90^\circ$$

$$\therefore \bar{S}_S = \bar{V}_S \bar{I}_S^*$$

$$\Rightarrow P_S + jQ_S = \frac{V_S^2}{X} |90^\circ - \frac{V_S V_R}{X} |90^\circ + \delta$$

$$\therefore P_S = \frac{V_S^2}{X} \cos 90^\circ - \frac{V_S V_R}{X} \cos(90^\circ + \delta)$$

$$\Rightarrow P_S = \frac{V^2}{X} \sin \delta \quad \dots(3)$$

$$\therefore Q_S = \frac{V_S^2}{X} \sin 90^\circ - \frac{V_S V_R}{X} \sin(90^\circ + \delta)$$

$$\Rightarrow Q_S = \frac{V^2}{X} - \frac{V^2}{X} \cos \delta \quad \dots(4)$$

$$\therefore P_{\text{loss}} = P_S - P_R = 0$$

$$\Rightarrow Q_{\text{loss}} = Q_S - Q_R = \frac{2V^2}{X} (1 - \cos \delta)$$

37. At lagging power factor voltage regulation is given by

$$\text{V.R.} = \frac{I_R}{V_R} (R \cos \theta + X \sin \theta)$$

$$= \frac{1}{Z_B} (R \cos \theta + X \sin \theta)$$

$$= \frac{R}{Z_B} \cos\theta + \frac{X}{Z_B} \sin\theta$$

$$= R_{pu} \cos\theta + X_{pu} \sin\theta$$

For maximum voltage regulation at lag p.f.

$$\frac{d(V.R.)}{d\theta} = 0$$

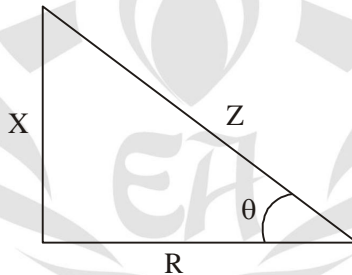
$$\Rightarrow R_{pu}(-\sin\theta) = X_{pu}(\cos\theta) = 0$$

$$\Rightarrow R_{pu} \sin\theta = X_{pu} \cos\theta$$

$$\Rightarrow \tan\theta = \frac{X_{pu}}{R_{pu}} = \frac{X/Z_B}{R/Z_B} = \frac{X}{R}$$

$$\therefore Z = \sqrt{R^2 + X^2}$$

$$\therefore \text{p.f.} = \cos\phi = \frac{R}{Z}$$



At leading power factor voltage regulation is given by—

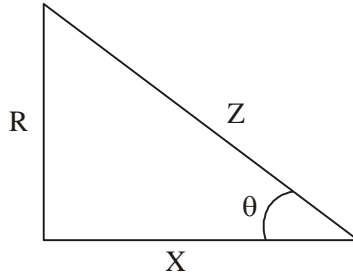
$$V.R. = \frac{I_R}{V_R} (R\cos\theta - X\sin\theta)$$

$$= \frac{1}{Z_B} (R\cos\theta - X\sin\theta)$$

$$= \frac{R}{Z_B} \cos\theta - \frac{X}{Z_B} \sin\theta$$

$$= R_{pu} \cos\theta - X_{pu} \sin\theta$$

For zero voltage regulation at lead p.f.



$$V.R. = 0$$

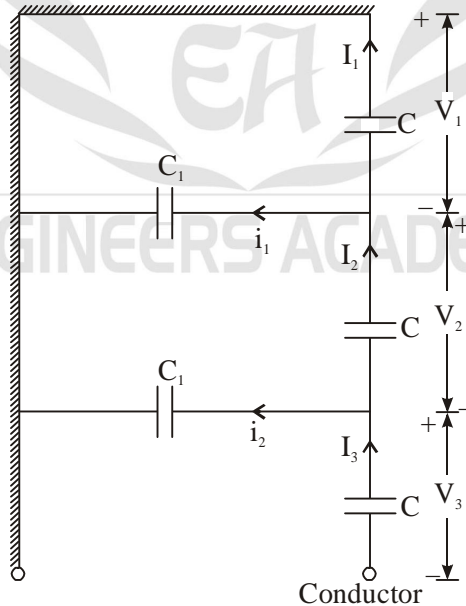
$$\Rightarrow R_{pu} \cos\theta = X_{pu} \sin\theta$$

$$\Rightarrow \tan\theta = \frac{R_{pu}}{X_{pu}} = \frac{R/Z_B}{X/Z_B} = \frac{R}{X}$$

$$\therefore \text{p.f.} = \cos\theta = \frac{X}{Z}$$

- 38.** Suspension type line insulators consist of number of porcelain discs connected in series by metal links in the form of a string. Each unit or disc is designed for low voltage and number of disc depend upon working voltage.

Potential distribution over suspension insulator string :-



Where, C = Self capacitance of insulator.

C_1 = Mutual or stray capacitance

Let $\frac{C_1}{C} = K$

$\therefore I_2 = I_1 + i_1$

$\Rightarrow \omega c V_2 = \omega c V_1 + \omega c_1 V_1$

$\Rightarrow C V_2 = C V_1 + (K C) V_1$

$\Rightarrow V_2 = V_1(1 + K)$

Due to presence of stray capacitance unequal current and voltage distribution along the each disc of string i.e., $V_1 < V_2 < V_3$.

$\therefore I_3 = I_2 + i_2$

$\Rightarrow \omega c V_3 = \omega c v_2 + \omega(KC)(V_1 + V_2)$

$\Rightarrow V_3 = K V_1 + (1 + K) V_2$

$\Rightarrow V_3 = K V_1 + (1 + K)(1 + K) V_1$

$\Rightarrow V_3 = (1 + 3K + K^2) V_1$

This unequal potential distribution represent by string efficiency

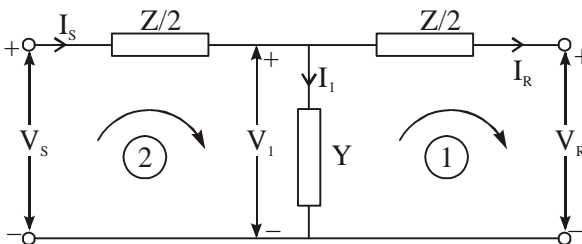
$$\eta = \frac{\text{Voltage across the string}}{\text{Number of disc} \times \text{Voltage across lowest disc}}$$

$$= \frac{V}{n \times V_n} \times 100\% = \frac{V}{3 \times V_3} \times 100\% \quad [\text{if } n = 3]$$

To improve string efficiency i.e. for equal distribution of voltage along the string.

- Using longer cross arm
- Using insulation grading ($c_1 < c_2 < c_3$)
- Using guard ring

39. T-model of medium transmission line.



Apply KVL in loop (1)

$$V_1 = V_R + \frac{Z}{2}I_R$$

$$\therefore I_1 = YV_1 = YV_R + \frac{YZ}{2}I_R$$

$$\therefore I_S = I_1 + I_R$$

$$\Rightarrow I_S = YV_R + \left(1 + \frac{YZ}{2}\right)I_R$$

Compare with

$$I_S = CV_R + DI_R$$

$$C = Y$$

$$D = 1 + \frac{YZ}{2}$$

Apply KVL in Loop (2)

$$V_S = V_1 + \frac{Z}{2}I_S$$

$$V_S = \left(V_R + \frac{Z}{2}I_R\right) + \frac{Z}{2}\left[YV_R + \left(1 + \frac{YZ}{2}\right)I_R\right]$$

$$V_S = \left(1 + \frac{YZ}{2}\right)V_R + Z\left(1 + \frac{YZ}{4}\right)I_R$$

Compare with

$$V_S = AV_R + BI_R$$

$$A = 1 + \frac{YZ}{2}$$

$$B = Z\left(1 + \frac{YZ}{4}\right)$$

